Pythagoras' Theorem

$$
c^{2}=a^{2}+b^{2}
$$

Trigonometric Ratios
Rules that Can be Used With Right-Angled Triangles

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Triangle Notation

For right-angled triangles only

$$
c^{2}=a^{2}+b^{2}
$$

Pythagoras' Theorem
Used to find the length of the third side when the other 2 sides are known

Sine (sin), cosine (cos) and tangent (tan) are ratios of two sides in a right-angled triangle.

Trigonometric Ratios
$\sin \theta=\frac{\text { length of the opposite side }}{\text { length of the hypotenuse }}=\frac{O}{H}$

Sine Ratio

$\cos \theta=\frac{\text { length of the adjacent side }}{\text { length of the hypotenuse }}=\frac{A}{H}$

Cosine Ratio

$\tan \theta=\frac{\text { length of the opposite side }}{\text { length of the adjacent side }}=\frac{O}{A}$
Tangent Ratio

$$
\tan \theta=\frac{\sin \theta}{\cos \theta}
$$

Relationship Between Sine, Cosine and Tangent

To find the value of a ratio
To find $\theta$ when 2 lengths are known
To find a length when another length and $\theta$ are known

## When Do We Use Trigonometric Ratios?

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Summary of Trigonometric Ratios

If $\sin \theta=$ number
angle ratio of 2 side lengths
Relationship Between an Angle and a Ratio


Use Pythagoras' Theorem to calculate the length of the third side.

Use a trigonometric ratio to find one of the angles.

Finding All Missing Angles and
Sides of a Triangle When 2 Sides are Known
Find the last angle by subtracting known angles from $180^{\circ}$.

Use a trigonometric ratio to find the length of one missing side.

Use Pythagoras' Theorem to calculate the length of the third side.

Find the last angle by subtracting known angles from $180^{\circ}$.

Finding All Missing Angles and Sides of a Triangle When 1 Side and 1 Angle are Known


## SOH CAH TOA Pyramids

3, 4, 5
5, 12, 13
7, 24, 25
8, 15, 17

## Common Triplets

where the longest side is the hypotenuse.

If a triplet exists, the triangle must be a right-angled triangle and therefore, $c^{2}=a^{2}+b^{2}$.

Pythagoras' Theorem
and Triplets

$$
\begin{aligned}
& \cos 30^{\circ}=\frac{\sqrt{3}}{2} \\
& \sin 30^{\circ}=\frac{1}{2} \\
& \tan 30^{\circ}=\frac{1}{\sqrt{3}}
\end{aligned}
$$

## Exact Values Based on $30^{\circ}$

$\cos 45^{\circ}=\frac{1}{\sqrt{2}}$
$\sin 45^{\circ}=\frac{1}{\sqrt{2}}$
$\tan 45^{\circ}=1$
Exact Values Based on $45^{\circ}$
$\cos 60^{\circ}=\frac{1}{2}$
$\sin 60^{\circ}=\frac{\sqrt{3}}{2}$
$\tan 60^{\circ}=\sqrt{3}$
Exact Values Based on $60^{\circ}$
$\cos 0^{\circ}=1$
$\sin 0^{\circ}=0$
Exact Values Based on $0^{\circ}$
$\tan 0^{\circ}=0$

```
cos90
sin}9\mp@subsup{0}{}{\circ}=
tan90
```

    Exact Values Based on \(90^{\circ}\)